

Titre : Contraintes, efforts, forces et déformations Responsable : Sébastien FAYOLLE Date : 22/03/2011 Page : 1/15 Clé : U2.01.05 Révision : 5955

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### Stresses, forces, forces and Résumé

#### strains:

This document defines the quantities characterizing the stresses, the forces and the strains inside a structure in a computation by finite elements in displacement and how that is translated in *Code\_Aster*. The statement of these quantities is given for the finite elements of mechanics: continuum 2D or 3D, shells and beams.

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# Code Aster

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#### Statique 1

#### 1.1 Contraintes

the postulate of Cauchy is that the forces of contacts exerted in a point by part of a continuum on another depends only on the norm on the surface in this point delimiting the parts.

In accordance with this postulate, one calls vector forced, for the nonmicropolar mediums,  $\mathbf{F}(\mathbf{n})$  the vector which characterizes the forces of contact exerted through a surface element DS of norm  $\mathbf{n}$  on part of a continuum [bib1].

It is shown [bib3], then, that the dependence in a point built-in from  $\mathbf{F}$  report with the norm  $\mathbf{n}$  is linear and that there exists a tensor which one calls tensor of the stresses  $\sigma$  such as:

$$\mathbf{F}(\mathbf{n}) = \boldsymbol{\sigma} \mathbf{n}$$

The unit of the stresses is it  $N_m^{-2} \equiv Pa$ .

For the group of structure "the stress state" is characterized by a field of tensor of the stresses which one more simply indicates by stress field.

#### 1.2 En ce qui concerne

force structures of beams or shells, contrary with the case of the continuum, it should be noted that:

- only the normal directions **n** of the cuts according to tangent space with the variety are possible.
- the characteristic quantities are obtained by integration in the section or the thickness of the guantities defined for the continuums.

#### 1.2.1 Cases of discrete

Les discrete are finite elements which can not have of a physical size. They are represented by their stiffness matrix. The forces are obtained by the multiplication of this matrix by the vector displacement:

$$\binom{F}{M} = [k] \cdot \binom{D}{R}$$

### 1.2.2 Case of the beams

One calls force, the end cells (F, M) in P, geometrical centre of inertia of the cross-section  $\Sigma$ , the torsor resulting from the forces of contact exerted on the section [bib2].

With the preceding notations:

$$F = \int_{\Sigma} \mathbf{F}(\tau) ds \qquad (N)$$
$$M_{p} = \int_{\Sigma} \mathbf{P} \mathbf{M} \wedge \mathbf{F}(\tau) ds \qquad (N \cdot m)$$

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For the beams whose cross-section is not regarded as rigid these end cells are not sufficient: for example, for the beams taking of account the warping of the sections one is brought to consider an additional quantity of force due to warping (bimoment).

The multifibre beams (with local behavior 1D, connecting stresses to strains, in a certain number of points of the section) and the pipes (local behavior in plane stresses) are comparable to conventional beam elements with regard to the motion of average fiber and the load vector forces resulting

### **1.2.3** Case of the shells

Soit, a point P of a surface medium S of thickness h, either an element length dl on S, or n the norm directing the shell in this point.

Maybe, end cells in this point (F, M) of a torsor resulting from the actions of contact exerted through a surface element dS = h dl of tangent n norm with S on part of S. With the preceding notations:



It is clear that M is in the tangent plane with S in P.

Either, N(P) the projection of F(P) on the tangent plane with S in P, and or, T(P) its normal component with this tangent plane.

In the same way that for the continuums, one shows that there exist two symmetric tensors N and M, and a vector Q, defined in the tangent plane with S, such as:

$$\mathbf{F} = N \mathbf{v}$$
$$T = Q \cdot \mathbf{v}$$
$$\mathbf{M} = \mathbf{n} \wedge M \mathbf{v}$$

(N, M, Q) the forces at the point are called P:

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- the tensor N characterizes the membrane forces,
- the tensor M, the bending moments,
- the vector Q, the shearing forces.

#### Note:

- There are no universal conventions on the denomination and the signs of these tensors. In particular, the tensor of the bending moments is taken with an opposite sign in the teaching of the ENPC and in practice of the French engineers of the civil engineer. Our convention is used in the great codex of finite elements (ANSYS) and makes it possible to have the same sign for a beam and a plate such as t = y.
- For curvilinear or surface structures out of material with nonlinear behavior, it is necessary to relocate the stress field in the section or the thickness, but the balance equations always relate to the fields of force. It is not necessary to go down again to the stresses to define L " stress state".

### **Restrains with the Dans**

stress field these conditions is a reference whose third component is carried by **n**, one has (  $\alpha$ ,  $\beta = 1$  ou 2):

$$N_{\alpha\beta} = N_{\beta\alpha} = \int_{-h/2}^{+h/2} \sigma_{\alpha\beta} dh$$
$$M_{\alpha\beta} = M_{\beta\alpha} = \int_{-h/2}^{-h/2} x 3 \sigma_{\alpha\beta} dh$$
$$Q_{\alpha} = \int_{-h/2}^{-h/2} \sigma_{\alpha3} dh$$

### 1.3 Nodal forces

One calls equivalent nodal force or more simply nodal force, a vector F which is the representative of a linear form W (generally dependent on an energy) acting on fields of displacement u(x) discretized by finite elements.

The fields of displacements u(x) are expressed starting from its nodal values which form a vector q and shape functions  $\Phi_i(x)$  by:

$$u(x) = \sum_{i} q_i \Phi_i(x)$$

Under these conditions:

$$w(u) = \sum_{i} q_{i} F_{i}$$

Note:

- The concept of node here is very general and wants to say, in fact, carrying degree of freedom (that it is of Lagrange or Hermite besides).
- The concept of displacement is also very general and includes the concept of generalized displacement including of the translations and rotations.

### 1.4 Representation of the fields

There are several ways of representing the fields in a modelization by finite elements:

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 for the continuous-current fields on all the field, one uses the values with the nodes, (CHAM\_NO of Aster)

$$\sigma(x) = \sum \sigma_i \Phi_i(x)$$

one speaks then about nodal stresses or nodal efforts,

### Remarque:

The stress fields or of forces are generally discontinuous, if they are represented way continuous it is only at ends of visualization.

for the discontinuous fields between the elements *e*, one then uses the values in certain points characteristic of the element (Gauss points or nodes).
 One speaks then about nodal stresses by elements or nodal efforts by elements, or, of stresses to the Gauss points or nodal efforts.

In practice, for the discontinuous fields one uses:

- representations with the nodes at ends of direct uses of the results (printing or postprocessing of visualization),
- at the Gauss points (or in what holds place of it), to continue computations requiring the true "stress state" in the element: geometrical rigidity, nodal force, nonlinear computations.

### 1.5 Quantities associated in Aster

### 1.5.1 SIEF\_R

quantity  ${\tt SIGM_R}$  represents the "stress state" of structure, therefore it must have, at least, the components:

stress fields of the continuums (in total reference):

SIXXSIYYSIZZSIXYSIXZSIYZ

• of the fields of forces of beam and discrete (out of local coordinate system with the beam, discrete):

NVYVZMTMFYMFZ

• for the beams with warping, it is necessary to add bimoment (necessarily out of local coordinate system with fiber):

ΒX

• of the fields of forces of shell (necessarily out of local coordinate system on the surface):

NXXNYYNXYMXXMYYMXYQXQY

Moreover, it is sometimes convenient to be able to directly exploit the fields of forces of beam and discrete in the total reference:

FXFYFZMXMYMZ

It is also interesting to represent the components of a stress field on the beam elements or shells in the local coordinate system. For that, one will use the same components as in total reference, although confusion is possible. In the future, one will introduce a concept of reference of representation attached to the fields which will overcome the difficulty.

### 1.5.2 FORC\_F and FORC\_R

Ces quantities represent the applied forces with structure on an application interface. For:

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- a continuum it is thus a force vector,
- a beam, a torsor of forces,
- a shell, a torsor of forces.

This quantity must thus have the following components:

• for a continuum:

FXFYFZ

• more for the beams and the shells:

MXMYMZ

### 1.5.3 DEPL\_R

Étant donné que in Aster,

- field can be attached only to only one quantity,
- that methods of finite elements mixed (mixing unknown of standard displacement and unknown factors of nodal the forces type) are not excluded,
- that the dualisation of the boundary conditions results in having for unknown a comprising vector of the variables of Lagrange which are nodal forces in the sense that it higher was specified,
- that it is necessary to be able to carry out any type of linear combination on the nodal forces,
- who the classification of the unknown factors must be the same one as that of the second members,

the nodal forces (dual within the meaning of energy w of nodal displacements) necessarily the same components have as displacements namely:

DXDYDZDRXDRYDRZ

more, for the beams with warping, bimoment: GRX.

### **1.6** Computation options

### 1.6.1 Computation of the "stress state"

### 1.6.1.1 Préfixe: SIEF\_ELGA

It acts of the options which calculate the field representative of the "stress state" and make it possible to continue computations (geometrical rigidity, nodal forces, etc.) in Gauss points or in what holds place of it. The prefix of these options is SIEF, because according to the elements, they compute stresses or forces.

Computation	Symbolic	Computation	3D, 2D,	Beams:	Plates:
option	name of result	carried out	COQUE 3D	POU_D_T	DKT
	concept		Coques1D	POU_D_E	DST
			PIPE	POU_D_TG	Q4G
			multifibre	POU_D_T_GD	
			Beams	Discrete	
SIEF_ELGA	idem	starting from a field of displacement in linear elasticity	σ	(F, M) out of local coordinate system	(N, M, V) out of local coordinate system
SIEF_ELGA	idem	starting from a complex field of displacement in linear elasticity	σ (C)	(F, M) out of local coordinate system (C)	(N, M, V) out of local coordinate system (C)

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RAPH_MECA FULL_MECA	SIEF_ELGA	into nonlinear	σ	(F, M) out of local coordinate system	σ
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Ces options thus calculate:

- the stress field for the elements of continuous medium 2D and 3D, and elements with local behavior: COQUE\_3D, shells 1D (COQUE\_AXIS, COQUE\_D\_PLAN, COQUE\_C\_PLAN), pipes, beams multifibre, in each "subpoint" of integration (layers in the thickness of the shells, fibers, sectors angular and position in the thickness for the pipes). The local coordinate system of the plates and shells is specific to each element,
- the field of forces for the beams (torsor) and the plates (tensor) into linear.

### 1.6.2 Other representations of the Préfixe

### 1.6.2.1 stress state: SIEF\_ELNO

It acts of the options which calculate the field representative of the "stress state" at ends of exploitation (printing or postprocessing of visualization) to the nodes of structure.

Computation option	Symbolic name of result concept	Computation carried out	3D, 2D	Beam, pipe, beam multi - fiber, Discrets	Shell, plate
SIEF_ELNO	idem	by interpolation with the nodes of the quantities at the Gauss points		$egin{array}{c} (F,M) \\ \mbox{out} & \mbox{of} & \mbox{local} \\ \mbox{coordinate} \\ \mbox{system} \end{array}$	(N, M, V) out of local coordinate system "user" (*)
SIEF_ELNO	idem	by interpolation with the nodes of the quantities at the Gauss points		$(F, M)_{out}$ of local coordinate system (C)	(N, M, V) out of local coordinate system "user" (C)

(\*) for the shell elements and of shell, the local coordinate system is that definite starting from the data of the user (key word ANGL REP in AFFE CARA ELEM).

### 1.6.2.2 Prefixes: SIGM ELNO

It acts of the options which calculate the stress fields whatever the modelization at ends of exploitation (printing or postprocessing of visualization) to the nodes of structure.

Computation option	Symbolic name of result concept	Computation carried out	3D, 2D	Beams	Shells, plates into 1 point chosen in the thickness (inf, moy, sup)
SIGM_ELNO	idem	starting from a field of displacement in linear elasticity	σ	$\sigma$ out of local coordinate system 6 components	$\begin{array}{c} \sigma \\ \text{out}  \text{of}  \text{local} \\ \text{coordinate} \\ \text{system} \\ \text{6 components} \end{array}$

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SIGM_ELNO	idem	starting from a complex field of displacement in linear elasticity	σ (C)	σ out of local coordinate system 6 components (C)	$\sigma$ out of local coordinate system 6 components (C)
SICA_ELNO	idem	out of total components (Cartesian) starting from the stress field out of local components	σ	σ in total reference	σ in total reference
SICA_ELNO	idem	out of complex total components (Cartesian) starting from the stress field out of complex local components	σ (C)	σ in reference room 6 components (C)	$\sigma$ out of local coordinate system 6 components (C)

### Remarques:

- 1) In this case, confusion is possible between the components out of local coordinate system and those in total reference which bear the same name.
- 2) The 6 components delivered in the local coordinate systems by the beams and the shells contain possibly null terms according to the models used. For the most standard models:
  - three null terms for the beams,
  - two null terms for the shells.

Thus, the stress field will be complete and, especially, it could be enriched each time the modelization requires it (beam with shears, shell with pinching, etc...)

#### **1.6.2.3 Prefixes:** EFGE\_ELNO

It acts of the options which calculate the forces on the beam elements or of shell at ends of exploitation (printing or postprocessing of visualization) to the nodes of structure.

Computation option	Symbolic name of result concept	Computation carried out	3D, 2Ds	Beams, pipes, beam multi - fibers, Discrets	Shells, plates
EFGE_ELNO	idem	starting from a field of displacement in linear elasticity	not	(F, M) out of local coordinate system	(N, M, V) out of local coordinate system
EFGE_ELNO	idem	starting from a complex field of displacement in linear elasticity	not	( <i>F</i> , <i>M</i> ) out of local coordinate system (C)	(N, M, V) out of local coordinate system (C)
EFCA_ELNO	idem	out of total components (Cartesian) starting from the field of forces out of local components	not	(F, M) in total reference	not

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EFCA_ELNO	idem	out of complex total components (Cartesian) starting from the field of forces out of complex local components	not	( <i>F</i> , <i>M</i> ) in total reference (C)	not

### 1.6.3 Computation of the nodal forces

### 1.6.3.1 Préfixe: FORC\_NODA

Les nodal forces are calculated starting from the "stress state", only one option is envisaged:

Computation option	Symbolic name of result concept	Computation carried out		3D	Beam	Shell
FORC_NODA	idem	starting from "SIEF_ELGA_*"	а	F	(F, M)	(F, M)

option REAC\_NO of operator CALC\_NO carries out a call to FORC\_NODA and withdrawn:

- the loading in statics,
- the loading, inertia forces and viscous in dynamics (in the facts, the viscous contribution in dynamics is currently neglected in CALC\_NO).

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### 2 Kinematics

### 2.1 Strains

### 2.1.1 Dans

Continuum this case, displacements of structure is represented by a field of vector  ${\tt U}$  to three components in general.

The strain (on the assumption of the small disturbances) is defined by the strain tensor  $\varepsilon$  by (option EPSI\_ELGA and EPSI\_ELNO):

$$\varepsilon_{ij}(u) = \frac{1}{2} (u_{i,j} + u_{j,i})$$

One can want to calculate the "mechanical" strain, i.e. by cutting off thermal dilations (options EPME\_ELGA and EPME\_ELNO):

$$\varepsilon_{ij}^{m}(u) = \frac{1}{2} (u_{i,j} + u_{j,i}) - \varepsilon^{th}$$

In the case of large displacements, the strains of Green-Lagrange are (options <code>EPSG\_ELGA</code> and <code>EPSG\_ELNO</code>):

$$E_{ij}(u) = \frac{1}{2} (u_{i,j} + u_{j,i} + u_{k,i} u_{k,j})$$

To which have can want to cut off the thermal strains (options EPMG ELGA and EPMG ELNO):

$$E_{ij}^{m}(u) = \frac{1}{2} (u_{i,j} + u_{j,i} + u_{k,i} u_{k,j}) - \varepsilon^{th}$$

### 2.1.2 Case of the beams

Dans the traditional beam theories, each point P of the beam represents a cross-section. In fact thus, the cells end of the torsor  $(T(s), \Omega(s))$  of displacement of the presumedly rigid cross-section characterize the displacement of the point P to the curvilinear abscisse  $s \cdot T$  is the translation of the centre of inertia of the section,  $\Omega(s)$  the vector rotation of the section in this point.

The application of the theorem of the virtual wors (cf [bib2]) naturally led to define as strain the torsor  $(\varepsilon, \chi)$  derived from  $(T(s), \Omega(s))$  report to the curvilinear abscisse s:



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Let us pose then:

$$\varepsilon = \varepsilon_L \tau + \gamma_T$$
$$\chi = \gamma_t \tau + \mathbf{K}$$

 $\varepsilon_L$  is the longitudinal deflection,

- $\gamma_T$  is the vector of the strains of distortion (no one on the assumption of Navier-Bernoulli),
- $\gamma_t$  is the strain of torsion of the section,
- K is the strain of bending.

#### Note:

For the modelizations of beam with taking into account of warping, the kinematics are more intricate to describe, but they lead however to concepts close to those presented above.

### 2.1.3 Case of the Nous

shells we will limit here to the cases of the plates. Indeed, in the general case of the shells:

- the spatial derivatives use too intricate mathematical concepts for the frame of this document, [R3.07.04],
- the shells are very often modelized by shell elements assembled.

In this case, in fact only the material norms are supposed to be rigid. The displacement of these norms is thus represented by the end cells of a torsor  $(T, \Omega)$ . T is the translation of the point located on the average layer,  $\Omega$  the vector rotation of the norm in this point.

It is clear that the normal component of  $\Omega$  is null (in the case of nonmicropolar mediums). One introduces, the vector I in the tangent plane defined by:

$$\mathbf{I} = \Omega \wedge \mathbf{n}$$

where n is the normal vector directing surface.



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Maybe, decomposition:

$$T = w \mathbf{n} + \mathbf{u}_{\tau}$$

- $\mathbf{u}_T$  is tangent displacement,
- w is the deflection.

In the same way that for the beams, the application of the theorem of the virtual wors (cf [bib2]) led to define as strain the whole formed by the tensors E and K the vector  $\gamma$  all these quantities being defined in the tangent plane by:

$$E_{\alpha\beta} = \frac{1}{2} (u_{\alpha,\beta} + u_{\beta,\alpha})$$
$$K_{\alpha\beta} = \frac{1}{2} (l_{\alpha,\beta} + l_{\beta,\alpha})$$
$$y_{\alpha} = l_{\alpha} + w_{\alpha}$$

The strain is thus defined by 7 realities.

 $E_{\alpha\beta}$  are the membrane strains,

 $K_{_{\alpha\beta}}$  are the opposite of the curvatures of the deformed average layer,

 $\gamma_{\alpha}$  is the vector of strain of distortion.

#### Note:

There still, there is no universal convention and the disparity of conventions is even larger than for the tensors of forces. The ENPC adopts an opposite convention for the tensor K for obvious geometrical ratios.

#### Restrain with the three-dimensional strain field

Dans these conditions, one a:

$$\varepsilon_{\alpha\beta} = E_{\alpha\beta} + x_3 K_{\alpha\beta}$$
  

$$\varepsilon_{\alpha3} = \gamma_{\alpha}$$
  

$$\varepsilon_{33} = 0$$

### 2.2 Quantities associated in Aster

### 2.2.1 DEPL\_R and DEPL\_C

Les quantities  $DEPL_R$  and  $DEPL_C$  have as components the degrees of freedom of the modelization by finite elements and thus do not have necessarily only the components of the fields of displacement which are:

DXDYDZ

with which it is necessary to associate for the beams or the shells:

#### DRXDRYDRZ

Pour the shells, we need the three components of the instantaneous axis of rotation, because the equation with the finite elements can be expressed only in one total cartesian coordinate system.

### 2.2.2 EPSI R

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quantity  ${\tt EPSI_R}$  represents the structural deformations  $% {\tt SIIR}$  , therefore it must have, at least, the components:

• strain fields  $\varepsilon$  of the continuums (in total reference):

EPXXEPYYEPZZEPXYEPXZEPYZ

• of the strain fields of beam (out of local coordinate system with the beam):

EPXXGAXYGAXZKYKZGAT

• of the strain fields of shell (necessarily out of local coordinate system on the surface)

EXXEYYEXYKXXKYYKXYGAXGAY

### 2.3 Préfixes

### 2.3.1 Computation options: EPSI\_ELGA, EPME\_ELGA, EPSG\_ELGA, EPMG\_ELGA

They is the options which calculate the strain fields at the points of integration of the elements.

Computation option	Symbolic name of result concept	Computation carried out	3D	Pipes, Beams multi_fibres	Shells, plates
EPSI_ELGA	idem	starting from a field of displacement in small strains	ε	$\varepsilon$ out of local coordinate system 6 components	not
EPSG_ELGA	idem	Tensor of Green- Lagrange starting from a field of displacement	Ε	not	
EPME_ELGA	idem	starting from a field of displacement and a field of temperature in small strains	ε	not	
EPMG_ELGA	idem	Tensor of Green- Lagrange starting from a field of displacement and of a field of temperature	$E^{m}$	not	

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### 2.3.2 Préfixe: EPSI\_ELNO, EPME\_ELNO, EPSG\_ELNO, EPMG\_ELNO

They is the options which calculate the strain fields whatever the modelization at ends of exploitation (printing or postprocessing of visualization) to the nodes of structure.

Computation option	Symbolic name of result concept	carried out	3D	Beams, Pipes, Beams multi_fibres	Shells, plates into 1 point chosen in the thickness (inf, moy, sup)
EPSI_ELNO	idem	starting from a field of displacement in small strains	ε	$\varepsilon$ out of local coordinate system 6 components	$\varepsilon$ out of local coordinate system: 6 components
EPSG_ELNO	idem	Tensor of Green- Lagrange starting from a field of displacement	Ε	not	
EPME_ELNO	idem	starting from a field of displacement and a field of temperature in small strains	ε <sup>m</sup>	not	
EPMG_ELNO	idem	Tensor of Green- Lagrange starting from a field of displacement and of a field of temperature	$E^m$	not	

### 2.3.3 Préfixe: DEGE\_ELNO

It acts of the options which calculate the strains generalized on the beam elements or of shell at ends of exploitation (printing or postprocessing of visualization) to the nodes of structure.

Computation option	Symbolic name of result concept	Computation carried out	3D	multifibre Beams, beams	Plates, Coques1D
DEGE_ELNO	idem	starting from a field of displacement in small strains	not	$(\varepsilon, \chi)$ out of local coordinate system	$(\boldsymbol{E}, \boldsymbol{K}, \boldsymbol{\gamma})$ out of local coordinate system

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